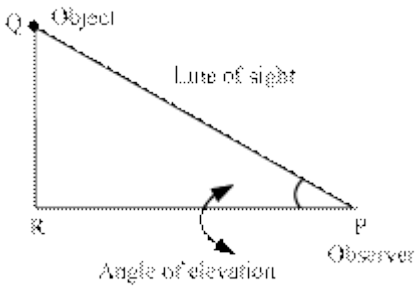
Some Applications of Trigonometry

- **Some Applications of Trigonometry**
  - **Line of sight:** It is the line drawn from the eye of an observer to a point on the object viewed by the observer.
  - **Angle of Elevation:**



Let P be the position of the eye of the observer. Let Q be the object above the horizontal line PR.
Angle of elevation of the object Q with respect to the observer P is the angle made by the line of sight PQ with the horizontal line PR. That is, ∠QPR is the angle of elevation.

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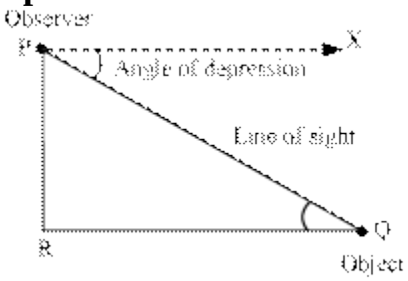
  - **Angle of Depression**



Let P be the position of the eye of the observer. Let Q be the object below the horizontal line PX.
Angle of depression of the object Q with respect to the observer P is the angle made by the line of sight PQ with the horizontal line PX. That is, ∠XPQ is the angle of depression. It can be seen that
∠PQR = ∠XPQ [Alternate interior angles]
The height or length of an object or the distance between two distant objects can be calculated by using trigonometric ratios.

Example:

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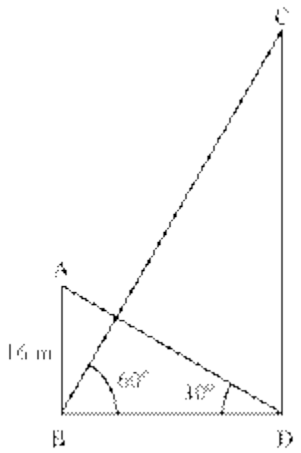
The angle of elevation of the top of a tower from the foot of a building is 60° and the angle of elevation of the top of the building from the foot of the tower is 30°. If the building is 16 m tall, then what is the height of the tower?

Solution:



Let AB and CD be the building and the tower respectively.
It is given that, angles of elevation ∠ADB = 30°, ∠CBD = 60°
In ΔABD,

$$\frac{AB}{BD} = \tan 30^\circ$$

$$\Rightarrow \frac{16}{BD} = \frac{1}{\sqrt{3}}$$

$$\Rightarrow BD = 16\sqrt{3}\ \text{m} \qquad \text{...(1)}$$

Now, in ΔCBD

$$\frac{CD}{BD} = \tan 60^\circ$$

$$\Rightarrow \frac{CD}{16\sqrt{3}} = \sqrt{3} \qquad [\text{using (1)}]$$

$$\Rightarrow CD = 16\sqrt{3} \times \sqrt{3}\ \text{m} = 48\ \text{m}$$

Thus, the height of the tower is 48 m.

Example:

Two wells are located on the opposite sides of a 18 m tall building. As observed from the top of the building, the angles of depression of the two wells are 30° and 45°. Find the distance between the wells. [Use $\sqrt{3} = 1.732$]

Solution:

The given situation can be represented as

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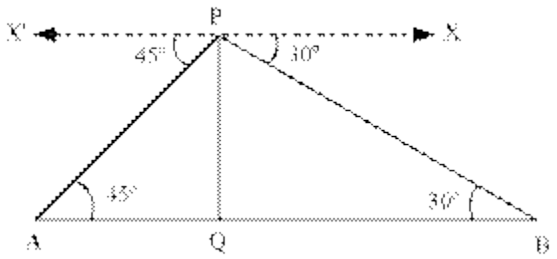

Here, PQ is the building. A and B are the positions of the two wells such that:
$\angle XPB = 30°$, $\angle XPA = 45°$
Now, $\angle PAQ = \angle XPA = 45°$
$\angle PBQ = \angle XPB = 30°$

In ΔPAQ, we have

$$\frac{PQ}{AQ} = \tan 45°$$

$$\Rightarrow \frac{18}{AQ} = 1$$

$$\Rightarrow AQ = 18\,m$$

In ΔPBQ, we have

$$\frac{PQ}{QB} = \tan 30°$$

$$\Rightarrow \frac{18}{QB} = \frac{1}{\sqrt{3}}$$

$$\Rightarrow QB = 18\sqrt{3}$$

$$\therefore AB = AQ + QB = \left(18 + 18\sqrt{3}\right) m$$

$$= 18\left(1 + \sqrt{3}\right) m$$

$$= 18(1 + 1.732) m$$

$$= 18 \times 2.732\ m$$

$$= 49.176\ m$$

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